

# ON-LINE TOOL FOR ANALYSIS OF SINGULAR STRESSES AND DISPLACEMENTS IN ANISOTROPIC MULTI-MATERIAL CORNERS

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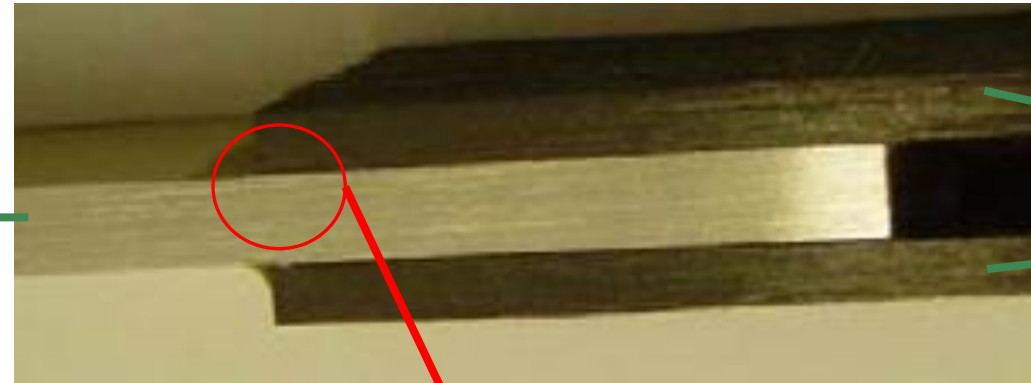
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# MOTIVATION

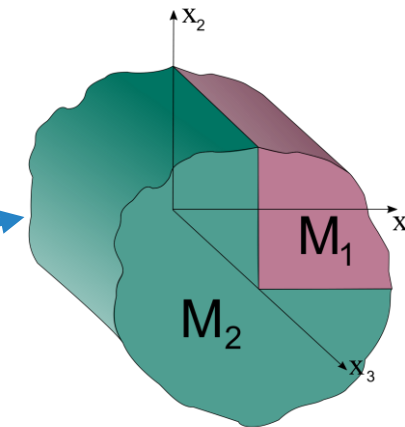
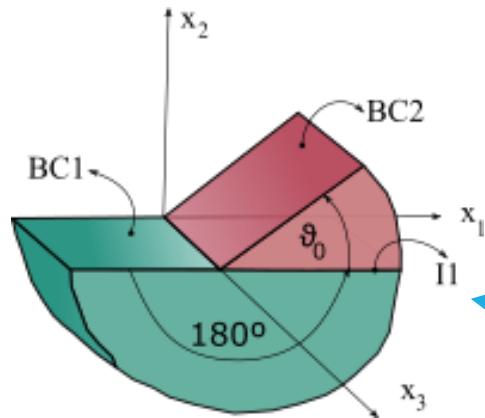


What do we have here?

Aluminum  
plate



Carbon fibre  
composite



# MOTIVATION



What do we have here?

Material discontinuities

Boundary or interface condition  
discontinuities

Geometry discontinuities

The theory of linear elasticity predict unbounded stresses where **failure** can be initiated

Local analysis of the stress field is recommended in these **SINGULAR POINTS**



## State of the art

### Particular expressions for the stress fields:

- Sinclair (2004): Solution for uni-material and multi-material isotropic corners. Different boundary conditions
- Chen et al.(2012), Poonsawat et al. (2010)... particular geometries of anisotropic materials corners

| General CODES                       | Single and Multi-material | Isotropic and anisotropic | General boundary conditions                         | General interface conditions                 | Dimension |
|-------------------------------------|---------------------------|---------------------------|-----------------------------------------------------|----------------------------------------------|-----------|
| Papadakis<br>Babuska (1995)         | ✓                         | ✓                         | ✗ Neumann or Dirichlet                              | ✗ Perfectly bonded                           | 2D        |
| Yosibash (1997)                     | ✓                         | ✓                         | ✗ Neumann or Dirichlet                              | ✗ Perfectly bonded                           | 3D        |
| Costabel, Dauge<br>Lafranche (2001) | ✓                         | ✓                         | ✗ Neumann or Dirichlet                              | ✗ Perfectly bonded                           | 3D        |
| Lee, Barber<br>(2006)               | ✓                         | ✗ Only<br>Isotropic       | ✓ Traction-free, clamped<br>Frictionless Frictional | ✓ Bonded, Frictionless<br>Frictional contact | 2D        |

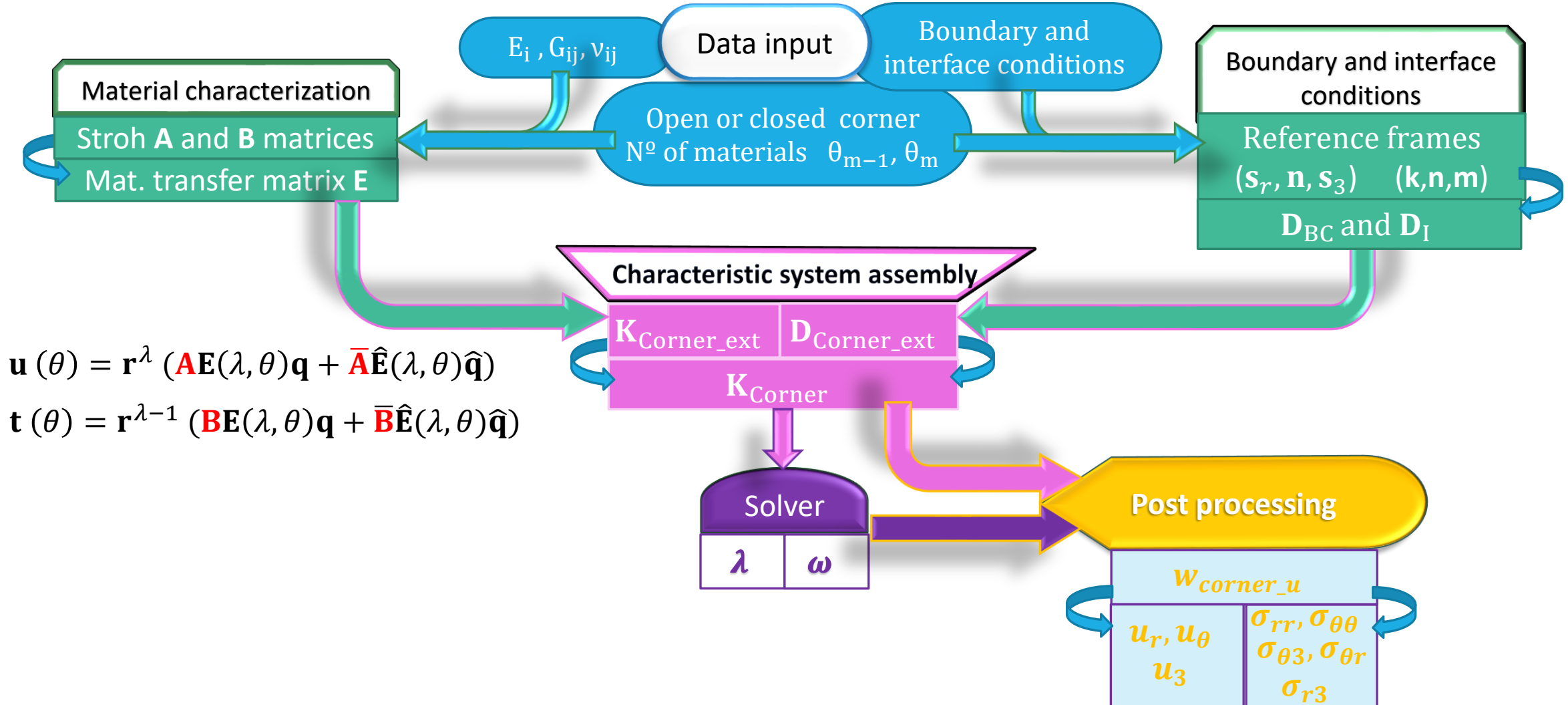
| General CODES                         | Single and Multi-material | Isotropic and anisotropic | General boundary conditions                                                  | General interface conditions                  | Dimension |
|---------------------------------------|---------------------------|---------------------------|------------------------------------------------------------------------------|-----------------------------------------------|-----------|
| Herrera, Mantic, Barroso (2022, 2023) | ✓                         | ✓                         | ✓ Traction-free, clamped, frictionless frictional, symmetry, antisymmetry... | ✓ Bonded, frictionless and frictional contact | 2.5D      |

## Objective of this work:

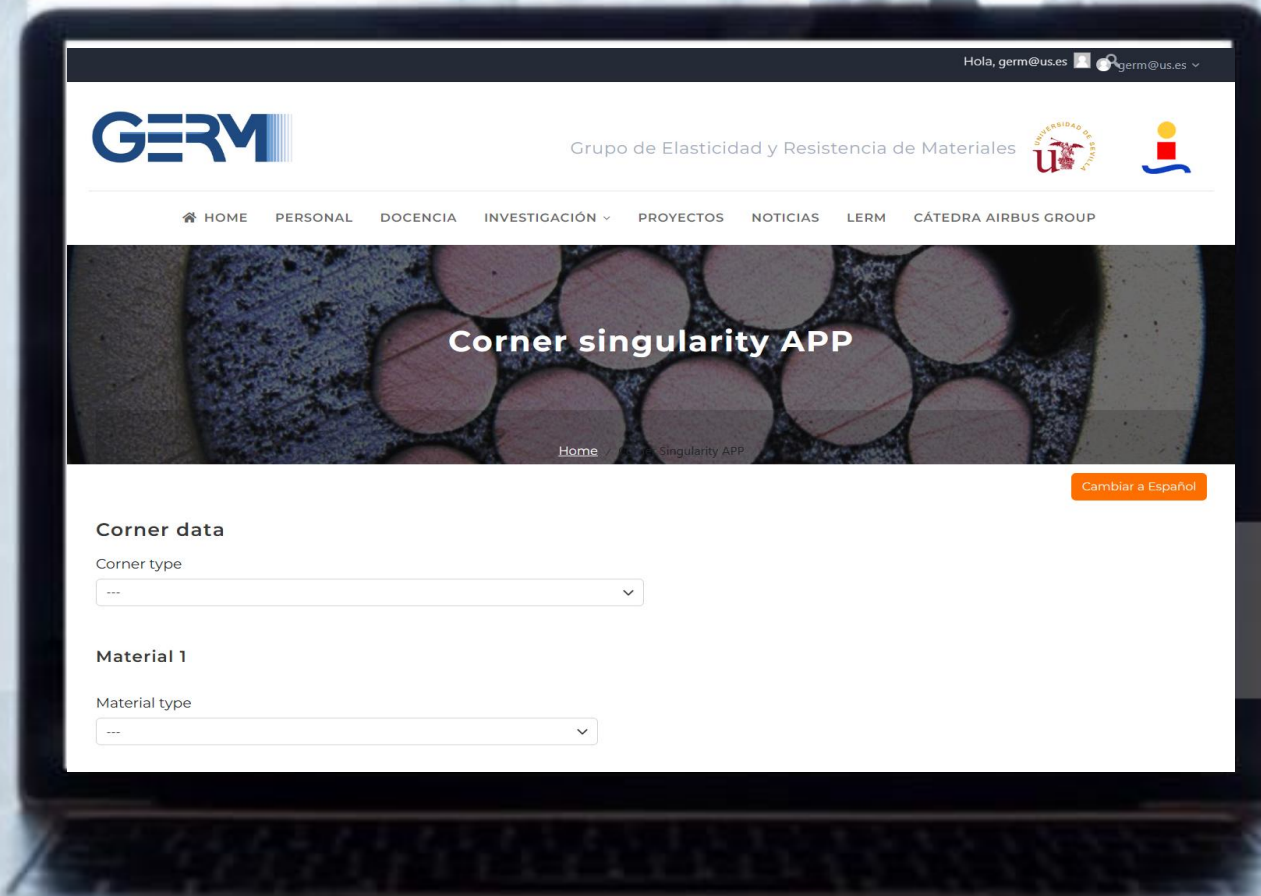
Present the **on-line tool** for analysis of singular points

Herrera, Mantic and Barroso, 2022 TAFMEC

Herrera, Mantic and Barroso, 2022 TAFMEC (under review)



Click to open the video



SINGULARITY RESULT: mensaje - Correo

Responder ... Probar el nuevo Outlook

## SINGULARITY RESULT

 **germsingularity@gmail.com** <germsingularity@gmail.com>  
21:45

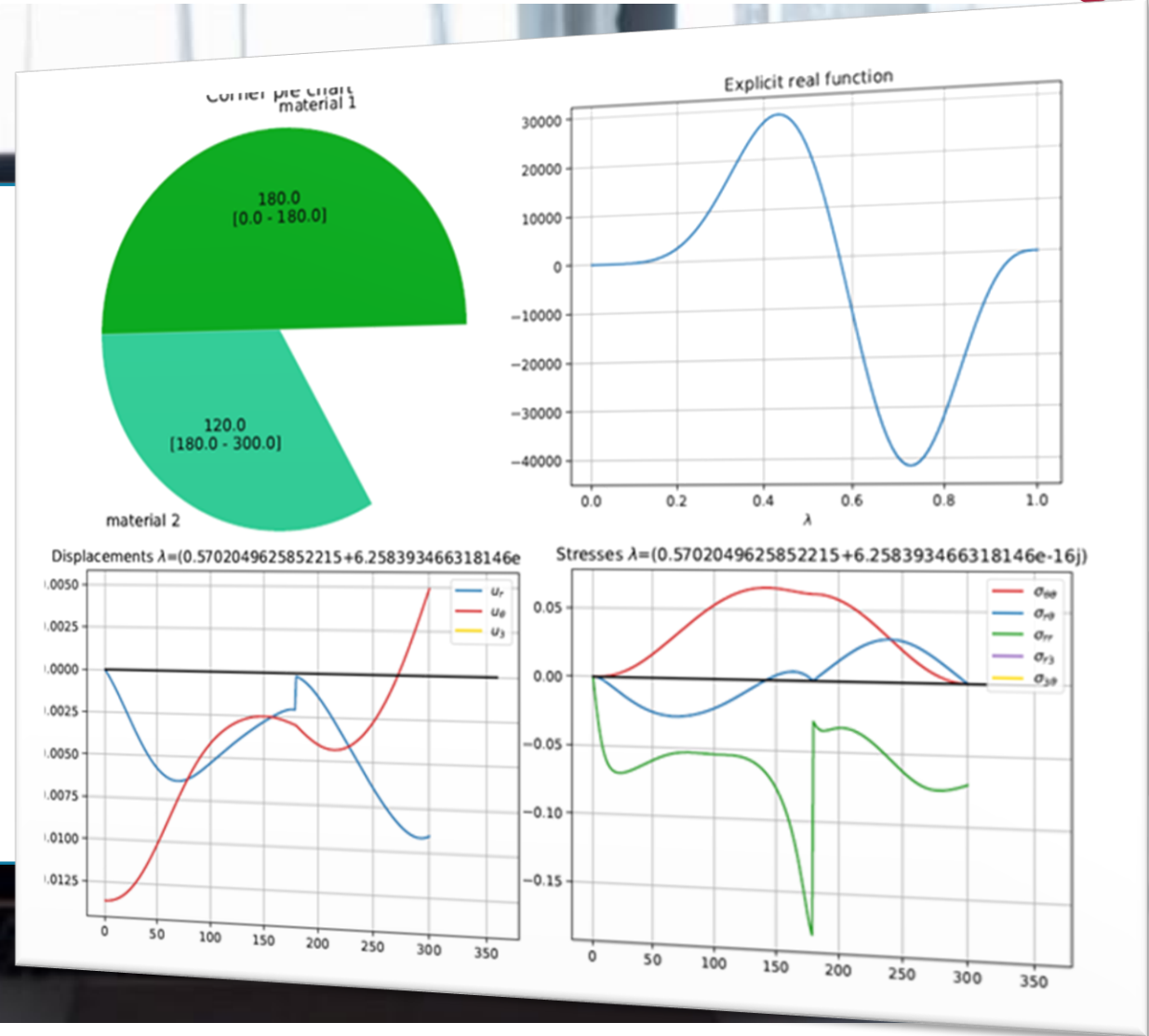
Para: MARIA ANGELES HERRERA GARRIDO

 **output.pdf**  
110,7 KB

Hello, here are the roots obtained for the requested corner:

0j  
(0.5702049625852215+6.258393466318146e-16j)

Please, do not reply to this email.



-A general code for singular stress and displacement analysis for isotropic or anisotropic multi-material corners with different boundary and interface condition has been developed

-The code is available in the following link:

<https://www.germus.es/corner-singularity-app/>

# Enjoy it!

# Thank you!



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<https://www.germus.es/corner-singularity-app/>

# Enjoy it!